

Chapter 6 Check List:

- 1 Sketching and identifying a Slope Field (p. 408)
- 2 Sketching a solution of a differential equation using a slope field (p 409)
- 3 Solving a differential equations (p 415)
- 4 Growth and decay models solving $\frac{dy}{dt} = ky$ (p 416)
- 5 Finding general and particular solutions to separable differential equations. (p 434-4)

Delta Math Check List:

- 1 Practice Slope Fields (6.1):
 - (a) Creating slope fields
 - (b) Solution Curves to Slope fields
 - (c) Slope field (Multiple choice)
- 2 Practice Diff-EQs (6.2-6.3)
 - (a) Tangent lines to Differential Equations
 - (b) Differential Equations (Level 1)
 - (c) Differential Equations (Level 2)

Khan Academy Check List:

Differential Equations Unit: 7 lessons, 3 Quizzes

- 1 Modeling situations with differential equations
- 2 Verifying solutions for differential equations
- 3 Sketching slope fields
- 4 Reasoning using slope fields
- 5 Finding general solutions using separation of variables
- 6 Finding particular solutions using initial conditions and separation of variables
- 7 Exponential models with differential equations
- 8 Videos explaining old AP Exam questions like 2011 AB 5

Always review your Notes and Examples (see topics if you lost your notes), Quizzes, and old homework problems. There is a separate pdf with Multiple choice practice as well.

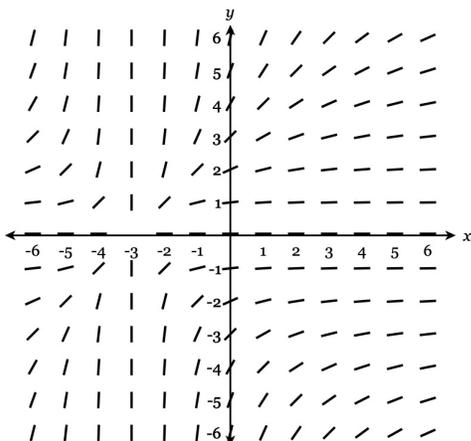
- (Calc OK) A sample of D1-13 (an isotope of Delirium) loses 99% of its radioactive matter in 199 hours. What is the half-life of D1-13?
 - 4 hours
 - 6 hours
 - 30 hours
 - 100.5 hours
 - 143 hours
 - None of these

- In which of the following models is $\frac{dy}{dt}$ directly proportional to y ?
 - $y = e^{kt} + C$
 - $y = Ce^{kt}$
 - $y = 28^{kt}$
 - $y = 3\left(\frac{1}{2}\right)^{3t+1}$
 - I only
 - II only
 - I and II only
 - II and III only
 - II, III, and IV only
 - All four

- (Calculator Active) The rate at which acreage is being consumed by a plot of kudzu is proportional to the number of acres already consumed at time t . If there are 2 acres consumed when $t = 1$ and 3 acres consumed when $t = 5$, how many acres will be consumed when $t = 8$?
 - 3.750
 - 4.000
 - 4.066
 - 4.132
 - 4.600
 - None of these

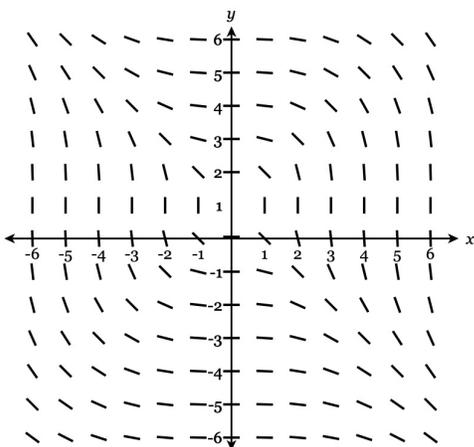
- Which of the following are separable differential equations? (There may be more than one)
 - $\frac{dy}{dx} = \ln(x + y)$
 - $\frac{dy}{dx} = e^{x+y}$
 - $\frac{dy}{dx} = x^2 + 3xy$
 - $\frac{dy}{dx} = xy + 4x$
 - None of these

5. Select the differential equation that matches the given slope field.



- (a) $\frac{dy}{dx} = -\frac{y}{x+3}$
 (b) $\frac{dy}{dx} = (x+3)y^2$
 (c) $\frac{dy}{dx} = \frac{x+3}{y}$
 (d) $\frac{dy}{dx} = \frac{y^2}{(x+3)^2}$
 (e) None of these

6. Select the differential equation that matches the given slope field.



- (a) $\frac{dy}{dx} = \frac{(y-1)^2}{x}$
 (b) $\frac{dy}{dx} = -\frac{x}{y-1}$
 (c) $\frac{dy}{dx} = -\frac{x^2}{(y-1)^2}$
 (d) $\frac{dy}{dx} = -\frac{y-1}{x}$
 (e) None of these

7. Which of the following is a solution of the differential equation $xy' - 4y = x^5e^x$?
- (a) $y = 4x^5e^{2x}$
 - (b) $y = 6e^{2x} - 7\sin 2x$
 - (c) $y = x^4e^x$
 - (d) $y = 5e^{-2x}$
 - (e) $y = \ln x$
 - (f) None of these
8. (a) (3 points) Consider the differential equation $\frac{dy}{dx} = xy^3$ with a particular solution $y = f(x)$ having an initial condition $y(-2) = -1$. Use the equation of the line tangent to the graph of f at the point $(-2, -1)$ in order to approximate the value of $f(-1.9)$.
- (b) (3 points) Consider the differential equation $\frac{dy}{dx} = (x^2 + 3)(y - 2)$ with a particular solution $y = f(x)$ having an initial condition $y(0) = -3$. Use the equation of the line tangent to the graph of f at the point $(0, -3)$ in order to approximate the value of $f(0.1)$.

9. Find the general solution to the following differential equations, then find the particular solution using the initial condition.

(a) $\frac{dy}{dx} = \frac{x}{y}$, $y(1) = -2$

(b) $\frac{dy}{dx} = -\frac{x}{y}$, $y(4) = 3$

(c) $\frac{dy}{dx} = \frac{y}{x}$, $y(2) = 2$

(d) $\frac{dy}{dx} = 2xy$, $y(0) = -3$

(e) $\frac{dy}{dx} = (y + 5)(x + 2), \quad y(0) = -1$

(f) $\frac{dy}{dx} = \cos^2(y), \quad y(0) = 0$

(g) $\frac{dy}{dx} = (\cos x)e^{y+\sin x}, \quad y(0) = 0$

(h) $\frac{dy}{dx} = e^{x-y}, \quad y(0) = 2$

(i) $\frac{dy}{dx} = -2xy^2, \quad y(1) = \frac{1}{4}$

(j) $\frac{dy}{dx} = \frac{4\sqrt{y} \ln x}{x}, \quad y(e) = 1$

10. Find the solution of the differential equation $\frac{dy}{dt} = ky$ that satisfies the given conditions, and use it to find another point.

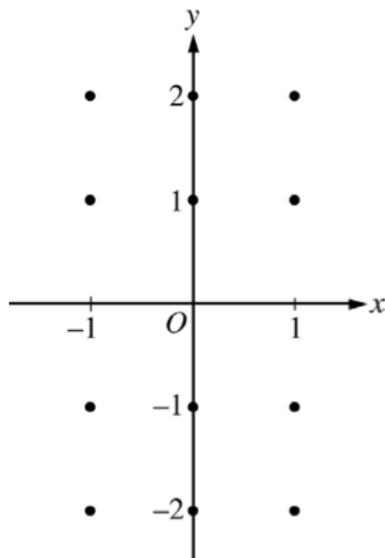
(a) $y(0) = 50$ and $y(5) = 100$. For what t is $y(t) = 75$?

(b) The graph of y passes through $(1, 55)$ and $(10, 30)$. Find $y(5)$.

11. Write and find a general solution of the differential equation that describes this statement: The rate of change of G with respect to t is proportional to $50 - t$.

12. (2010B AB 5 - No Calc) Consider the differential equation $\frac{dy}{dx} = \frac{x+1}{y}$.

- (a) (3 points) On the axes provided, sketch a slope field for the given differential equation at the twelve points indicated, and for $-1 < x < 1$, sketch the solution curve that passes through the point $(0, -1)$.

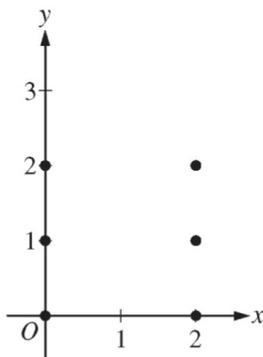


- (b) (1 point) While the slope field in part (a) is drawn at only twelve points, it is defined at every point in the xy -plane for which $y \neq 0$. Describe all points in the xy -plane, $y \neq 0$, for which $\frac{dy}{dx} = -1$.

- (c) (5 points) Find the particular solution $y = f(x)$ to the given differential equation with the initial condition $f(0) = -2$

13. (2016 AB 4 - No Calc) Consider the differential equation $\frac{dy}{dx} = \frac{y^2}{x-1}$.

- (a) (2 points) On the axes provided, sketch a slope field for the given differential equation at the six points indicated.

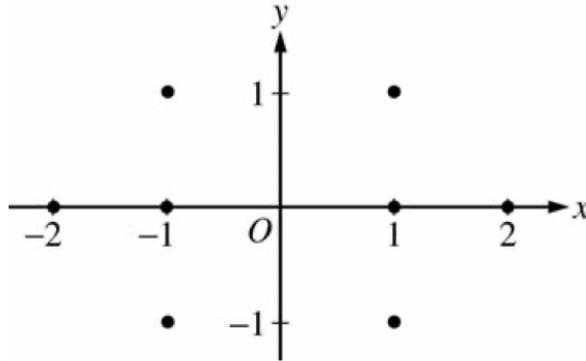


- (b) (2 points) Let $y = f(x)$ be the particular solution to the given differential equation with the initial condition $f(2) = 3$. Write an equation for the line tangent to the graph of $y = f(x)$ at $x = 2$. Use your equation to approximate $f(2.1)$.

- (c) (5 points) Find the particular solution $y = f(x)$ to the given differential equation with the initial condition $f(2) = 3$.

14. (2006 AB 5 - No Calc) Consider the differential equation $\frac{dy}{dx} = \frac{1+y}{x}$ where $x \neq 0$

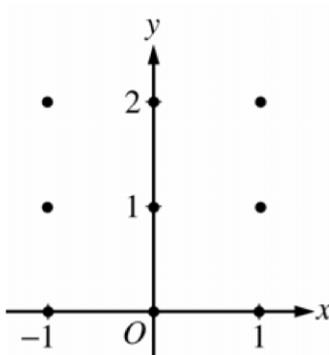
- (a) (2 points) On the axes provided, sketch a slope field for the given differential equation at the eight points indicated.



- (b) (7 points) Find the particular solution $y = f(x)$ to the differential equation with the initial condition $f(-1) = 1$ and state its domain..

15. (2007B AB 5 - No Calc) Consider the differential equation $\frac{dy}{dx} = \frac{1}{2}x + y - 1$.

- (a) (2 points) On the axes provided, sketch a slope field for the given differential equation at the nine points indicated.



- (b) (3 points) Find $\frac{d^2y}{dx^2}$ in terms of x and y . Describe the region in the xy -plane in which all solution curves to the differential equation are concave up.

- (c) (2 points) Let $y = f(x)$ be the particular solution to the differential equation with the initial condition $f(0) = 1$. Does f have a relative minimum, a relative maximum, or neither at $x = 0$? Justify your answer.

- (d) (2 points) Find the values of the constants m and b , for which $y = mx + b$ is a solution to the differential equation.